Automated Online Measurement of Particle Size Distribution using 3D Range Data

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Abstract: Fully automated online measurement of the size distribution of limestone fragments on conveyor belt is presented based on 3D range data collected every minute during 13 hours of production. The research establishes the necessary measurement technology to facilitate automatic control of particle breaking or aggregating processes to improve both energy efficiency and product quality. Techniques are presented covering; sizing of fragments, determination of non-overlapped and overlapped fragments, and mapping of sizing results to distributions comparable to sieving. Detailed variations in the product sieve size are shown with an abrupt change when the size range of the limestone fragments was changed.

Keywords: image segmentation, particle size measurement, range data, classification

1. INTRODUCTION

In the mining and aggregate industries a great deal of effort goes into measuring or estimating the size distribution of particulate material. One reason is that suppliers of particulate material are typically paid to supply a specific size range of material. For both industries there is also a key desire for energy efficiency and size quality that is relevant in both crushing and aggregating processes. In addition, blasting and caving are very cost effective methods of rock breakage, but they are not processes that are easily quantified.

Mine and quarry operators want to measure the particle sizing results of all of these activities but sieving is typically impractical as a routine assessment tool due to slow feedback, inconsistent measurement, and time consuming interruption.

As a result there is an opportunity for online, non-contact, fully automated machine vision systems for measurement of particle size that can provide the necessary accuracy and fast feedback to facilitate process control and allow automatic control optimisations for both product size and energy efficiency. This is relevant to a vast range of processes that modify particle size such as blasting, crushing, pelletising, and in ovens and kilns.

There are however, a number of sources of error relevant to techniques that measure only what is visible on the surface of a pile as follows;

Segregation and grouping error, more generally known as the brazil nut effect (Rosato et al., 1987), describes the tendency of the pile to separate into groups of similarly sized particles. It is caused by vibration or motion (for example as rocks are transported by truck or conveyor) with large particles being moved to the surface. It is advisable to measure at a point early on the conveyor before the material has been subjected to excessive vibration and segregation.

Overlapped particle error, describes the fact that many particles are overlapped (see figure 1) and only partially visible and a large bias to the smaller size classes results if they are treated as small non-overlapped and sized using only their visible profile. This error can be overcome in piles of particulate material using classification algorithms based on 3D range data (Thurley and Ng, 2008).

Fig. 1. Illustration of overlapped and non-overlapped particles.

Capturing error, describes the varying probability based on size, that a particle will appear on the surface of the pile. In simple terms, the larger a particle is, the more likely one is to be able to see some part of it on the surface. For example, if a single particle is as large as the height of the pile of material, then it will always be visible, whereas a very fine particle is almost certainly not visible. Thurley (2002) has explored capturing error in laboratory rock piles but it remains a source of error in this application.

Profile error, describes the fact that only one side (a profile) of an entirely visible particle can be seen making
if difficult to estimate the particles size. However, if the particle is not overlapped, best-fit-rectangle (Wang, 2006) has been demonstrated as a suitable feature for size classification based on the visible profile, that correlates to sieve size.

In addition to these errors, we note that size measurement using imaging identifies how many particles are observed of various size classes, but manual sieving measures the weight of particles in each size class. Therefore it is necessary to have a method of mapping from numbers of particles to weight of particles in order to provide a measurement of size that industry understands and can use. A technique based on physical sampling and sieving results is used in this work and explained in detail subsequently.

Particle size measurement using vision has been the subject of research and development for over 25 years (Carlsson and Nyberg, 1983) with a legacy of predominantly photographic based systems with widely varying degrees of success and no general solution available on the market.

Photographic based 2D imaging systems are subject to bias due to uneven lighting conditions, excessive shading, color and texture variation in the material, and lack of distinction between overlapped and non-overlapped fragments.

In their review of a commercial photographic based 2D system Potts and Ouchterlony (2005, pg. vi, viii) report that for their application the system erroneously assumes the resultant size distribution is unimodal and they conclude by expressing strong reservations saying 2D “imaging has a certain but limited usefulness when measuring the fragment size distribution in a mound or from a belt in an accurate way. It could probably detect rough tendencies in fragmentation variations, if the lighting conditions do not vary too much, and if cover glasses for camera lenses are kept clean”.

There are a number of publications relating to 3D size measurement, Noy (2006, rocks), Frydendal and Jones (1998, sugar beets), Kim et al. (2003, river rock) Lee et al. (2005). However, Frydendal and Jones (1998), and the presenting author Thurley and Ng (2008) are the only publications (2D or 3D) to remove the bias resulting from overlapped particles. For conveyor belt applications Kim et al. (2003) and Lee et al. (2005) recommend installing a mechanical vibration feeder to separate rocks and prevent particle overlap. However, such an addition to the plant is typically impractical and for the examination of rocks in buckets (Thurley, 2009), there is no other option than to account for overlapped and non-overlapped fragments. Frydendal and Jones (1998) used graph theory and average region height to determine the entirely visible sugar beets but this relied on the regular shape and size of the beets. Only the presenting author has made this distinction between overlapped and non-overlapped particles using the advantages of 3D range data and in a manner that does not presume constraints on size or shape (Thurley and Ng, 2008).

We use an industrial measurement system on conveyor belt based on laser triangulation (a projected laser line and camera triangulation) collecting highly accurate 3D profiles of the laser line at about 3000 Hz. This high speed ensures we have a high density of 3D point data at a spacing between consecutive points in the direction of the belt of approximately 1 mm. The imaging system is installed at a limestone quarry on the conveyor belt used for ship loading and measures the material on the belt during loading every minute.

The computational speed of the analysis process is approximately 53 seconds on a 2 GHz Mobile Pentium 4 processing a data set of 500,000+ 3D points (2 m long section of the belt). Furthermore, multi-core CPUs effectively offer a linear increase in the rate at which data could be sampled from the conveyor and processed. Further advances in both algorithmic efficiency and hardware are both available to improve computational time for rapid automatic control applications.

2. RESEARCH BACKGROUND

The presented research builds upon a series of achievements and research developed on both laboratory rock piles and industrial application.

We have previously implemented an industrial measurement system on conveyor belt for iron ore pellets (Thurley and Andersson, 2007) using the same laser triangulation measurement technology. The high speed camera system ensures we have a high density of 3D point data at a spacing between consecutive points in the direction of the belt of approximately 0.5 mm. This high data density has at least two advantages. Firstly it allows us to detect small sliver regions or crescent-like regions of overlapped particles and ensure that they are not merged into other regions. And secondly, it has ensured that we could detect a very high resolution when it came to measuring the size of each iron ore pellet allowing a size distribution with very fine spacing of 5, 8, 9, 10, 11, 12.5, 13, 14, and 16+ mm size classes.

One of the key criteria for particle size measurement is therefore high data density as it determines the capacity to detect small overlapped particles, the lower limit on particle size that can be reliably detected, and the resolution of size classes detectable.

Another criterion is the computational speed of the analysis. It is generally desirable in a conveyor belt situation to sample as frequently as possible, but a sufficient sampling rate depends on the specific application. In the presented application for limestone both the lower limit of particle size (about 10 mm) and the response time to deviations in size during ship loading (about 5 minutes) are well within the computational speed and resolution capabilities of the system.

In addition we have performed a demonstration project for size measurement of rocks in underground LHD excavator buckets Thurley (2009). A 3D vision system based on laser scanners was installed on the tunnel roof in a production area of an underground iron ore mine with 3D surface data of the bucket contents being collected as the LHD unit passes beneath. The project successfully demonstrated fragmentation measurement of the rocks in the bucket, identifying overlapped rocks, non-overlapped rocks, areas of fine material, estimating the sieve size of the visible
rocks only, and the calculating the proportion of the surface that was identified as fine particles below the observable resolution of the laser scanner.

3. ANALYSIS OF 3D RANGE DATA

3.1 Segmentation

The first step is to perform the detailed image segmentation to identify the individual rock fragments. These techniques have been applied to laboratory rock piles (Thurley and Ng, 2005) and in an industrial pellet measurement system (Thurley and Andersson, 2007) and were adapted to this application. The technique is predominantly based on morphological image processing, based largely on various edge detection techniques to facilitate seed formation for the watershed segmentation algorithm.

Figure 2 shows a closeup image of rocks on the conveyor and the automated segmentation result.

![Fig. 2. Rocks on conveyor and automated segmentation for limestone aggregate, 40–70 mm size range.](image)

3.2 Non-overlapped Particles

In order to explain the determination of overlapped and non-overlapped particles it is necessary to introduce a boundary following algorithm developed by Thurley and Ng (2008) for the purpose of overlapped particle detection.

The algorithm begins with a segmentation of a pile of particulate material and examines each region in the segmentation. For each region in the segmentation we identify a series of prominent points equally spaced around the perimeter of the region.

Looking at figure 3 we see a representation of two regions (one overlapping the other) with a series of prominent points marked for region $R_i$.

We then use these points to define small local areas in which we examine the height of the regions in that local area. In the magnified section of figure 3 you can see a circular area about point $g$, we examine this area, denoted $N_g$, and calculate the average height of all of the points in the region $R_i$ that intersect area $N_g$, and we calculate the average height of all of the points in the region $R_n$ that intersect region $N_p$. By comparing these two average height values we can evaluate whether in the local neighbourhood of point $g$, region $R_i$ is either above or below region $R_n$.

This determination is used to determine overlapped/non-overlapped particles by counting the ratio of points $g$ where region $R_i$ is above region $R_n$.

This distinction allows us to eliminate misclassification of overlapped rocks are if they were smaller non-overlapped rocks.

We apply an equivalent strategy to that applied on laboratory rock piles (Thurley and Ng, 2008) using the visibility ratio and selecting a decision boundary of 0.65. Figure 4 shows only the rocks that were classified as non-overlapped from figure 2.

We will perform sizing on the non-overlapped rocks for which we can make a confident size prediction, and we will ignore overlapped rocks.

![Fig. 3. Boundary following algorithm](image)

Fig. 3. Boundary following algorithm

![Fig. 4. Non-overlapped rocks automatically identified from figure 2, 40–70 mm size range.](image)

Fig. 4. Non-overlapped rocks automatically identified from figure 2, 40–70 mm size range.

3.3 Sizing

Sizing begins by calculating a feature called best-fit-rectangle area for each of the regions identified as non-overlapped fragments from the segmentation (figure4). The best-fit-rectangle is the rectangle of minimum area that fits around the 2D projection of each region. We ignore the height component of the points in a region and calculate an arbitrarily rotated best-fit-rectangle. We have used this feature previously (Thurley and Ng, 2008; Thurley and Andersson, 2007, laboratory rock piles, iron ore pellets) and demonstrated its suitability for estimating sieve size of non-overlapped particles.

In order to classify best-fit-rectangle areas into sieve size classes however, we require a series of decision boundaries.
In effect, thresholds that define which area values separate one size class from another. To determine these values we use some sieving data that corresponds to some of our image analysis results.

During the measurement campaign we collected a 3D data set of the surface of the rock stream every minute for approximately 13 hours of production. In this time we obtained just over 600 3D data measurement sets of limestone on the conveyor belt, and automatically identified and sized over 140,000 rocks. In addition, the mining company obtained some manual samples from the conveyor using a automated sampler, and subsequently sieved these in the laboratory. Table 1 shows these sieving results. What we see is that two distinct product ranges of material were being loaded at different times. Firstly the 40–70 mm product, then the 20–40 mm product, before changing back to the 40–70 mm. For a given sieving, most of the material is within the product size range, but there is always some small proportion above and below this range.

Table 1. Sieving results (cumulative %)

<table>
<thead>
<tr>
<th>Size (mm)</th>
<th>40–70mm</th>
<th>20–40 mm</th>
<th>40–70 mm</th>
</tr>
</thead>
<tbody>
<tr>
<td>&gt; 75</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 75</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 63</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 50</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 45</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 40</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 37.5</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 31</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>&lt; 25</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>12–20</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
</tbody>
</table>

We select two data sets from each product range (times 23:05, 00:15, 09:45, and 11:40) and use the sieving data and corresponding image analysis results to calculate decision boundaries for mapping best-fit-rectangle area into sieve size class.

We use the Nelder and Mead (1965) iterative error minimisation process to calculate decision boundaries with minimised error. This optimisation method is available both in Matlab using function fminsearch, or in the statistical package R using function optim which we use here. Given an initial estimate of the decision boundaries we use Nelder-Mead minimisation to produce a final set of boundaries.

The Nelder-Mead optimisation takes an estimate of the decision boundaries and calculates the error at that estimate (we define this error function in more detail in the next section). The optimisation modifies the decision boundaries slightly following a range of internal rules before repeating the process. Changes that reduce the error are kept, while changes that increase the error are typically discarded. We first calculate optimum decision boundaries for each set of sieving data and then calculate the median values as the initial estimates for the Nelder-Mead and generate the error minimised result.

Figure 5 shows the distribution of best-fit-rectangle (BFR) area measurements for the non-overlapped rocks calculated by the system for the two different products from all 600+ 3D measurements. We can clearly see that when the smaller product is on the belt, smaller values of the BFR area are generally calculated. We also show the location of the decision boundaries for each size on the bottom axis as calculated using the Nelder-Mead optimisation.

3.4 Mapping from Number to Weight

One of the complications for image analysis systems is that they can measure the number of observable particles, and using classification strategies for size can calculate number of particles in each size class. However, what is required is the estimated weight of the material in each size class as this percentage by weight is what is measured by sieving and required by industry. Therefore it is necessary to convert number of particles by size class into an estimated weight by size class. We do this by collecting sieving results and counting the number of particles in each size class in order to determine an average weight of a fragment by size class as shown in table 2.

Table 2. Mean Particle Weight by Size Class

<table>
<thead>
<tr>
<th>Size (mm)</th>
<th>Mid Size (mm)</th>
<th>Mean Particle Weight (g)</th>
</tr>
</thead>
<tbody>
<tr>
<td>&gt; 75</td>
<td>80</td>
<td>540</td>
</tr>
<tr>
<td>63–75</td>
<td>69</td>
<td>540</td>
</tr>
<tr>
<td>50–63</td>
<td>56.5</td>
<td>289</td>
</tr>
<tr>
<td>45–50</td>
<td>47.5</td>
<td>na</td>
</tr>
<tr>
<td>40–50</td>
<td>45</td>
<td>164</td>
</tr>
<tr>
<td>37.5–40</td>
<td>38.8</td>
<td>132</td>
</tr>
<tr>
<td>31–40</td>
<td>35.5</td>
<td>73.7</td>
</tr>
<tr>
<td>31–37.5</td>
<td>34.3</td>
<td>na</td>
</tr>
<tr>
<td>25–37.5</td>
<td>31.3</td>
<td>72.5</td>
</tr>
<tr>
<td>20–25</td>
<td>28</td>
<td>na</td>
</tr>
<tr>
<td>12–20</td>
<td>16</td>
<td>9.21</td>
</tr>
</tbody>
</table>

The immediate thing that one notes from table 2 is that different arrangements of sieve decks were used at different times (for the different products) complicating the capacity to compare and combine the results. As a result we calculate a polynomial of best-fit for the sieve mid-size versus weight. This provides a continuous and consistent estimate of weight for any given size class that we wish to estimate with the imaging.

Based on the data in table 2 we calculate a third order polynomial where x is the mid size of the sieve range and...
the weight is given by \( f(x) = 0.001208x^3 + 0.01494x^2 + 0.5306x \) with correlation \( R^2 = 0.9909 \). The graph of table 2 and the best-fit polynomial is not shown due to page limitations.

This mismatch between measuring numbers of particles and correlating against weight affects the Nelder-Mead error minimisation process. As a result we use the weights calculated using the best-fit polynomial within the Nelder-Mead error minimisation. We express this error function as a sum of squares as shown in equation (1). The function uses a normalized weight value derived from the polynomial weight function \( f \). The normalized weight provides a weight of 1 for the heaviest size class at a given time \( t \), with the lighter weights scaled relatively to this value. The purpose of this normalization is to ensure that heavier product ranges do not dominate the error function. Without this normalization the results for the 40-70mm product dominate the optimization effectively ignoring the error for the 20-40mm product.

\[
\begin{align*}
\epsilon &= \sum_t \sum_{x=1}^{N} \left( C_{x,t} - S_{x,t} \right)^2 / \max_x(f) \\
\hat{W}_{x,t} &= \frac{f(x)}{\max_x(f)} 
\end{align*}
\]  

(1)

Furthermore, as decision boundaries must be monotonically increasing with size class \( x \) (the larger the size class the larger the decision boundary), we must further constrain the error-function by using a penalization factor when the decision boundaries are out of order. Specifically we scale the error by the amount that any consecutive decision boundaries is out of order. Without this constraint the error minimization can generate meaningless out of order results.

Using the optimised Nelder-Mead decision boundaries for determining the sieve size class boundaries (depicted in figure 5) we produce estimates of the sieve size distributions for the 606 measurement sets. The results are presented in figure 7 with the sieve data from table 1 overlayed as colored points.

If we look only at the sieving results from 0:15 and 6:50, and the two imaging measurements that correspond to these times we can plot a typical log-linear cumulative size distribution curve as shown in figure 6.

4. DISCUSSION

The imaging results (figure 7) are shown to clearly trend in the right direction tracking changes in the material size. Furthermore, in the higher size classes, 50, 63, 75, where decision boundaries could be set for the 40-70 mm product independently of the 20–40 mm product, the imaging results appear to track the sieving results well.

Fig. 6. Imaging and sieving results for 2 measurements and sieve results at 0:15 and 6:50.

If we examine figure 7 and compare it to the cumulative sieving results in table 1 we can see that the image analysis overestimates the amount of < 40 mm size class in the 40–70 mm product, by about 10%, and underestimates the cumulative amount in the 20–40 mm product by about 25%.

The key problem is that an average weight by size class will work fine if the fragments are always uniformly distributed across that size class. The polynomial weight function attempts to produce a reasonable average weight by size class for all cases but further work is necessary to understand this relationship.

Improvements are expected after performing additional sieving experiments with a much finer sieving, using consistent decks for all products, such as 0, 12, 20, 25, 31, 37, 40, 45, 50, 63, 75 etc. instead of changing the decks as was done here. This sort of high resolution sieving will be carried out in an upcoming measurement and sieving trial to collect the necessary field measurements so that we can more accurately represent fragment weight variations by size class.

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REFERENCES

Sieve Size Distribution 606 measurements (5 sample average)

Fig. 7. Imaging and sieving results for 606 measurements over 10 hours of loading.


